

Continue

Arithmetic Sequence Calculator

This calculator uses the following formula to find the n-th term of the sequence:

$$a_n = a_1 + (n - 1)d$$

Enter any two values:

Arithmetic Progression
Definition: An arithmetic progression is a sequence of the form: $a, a + d, a + 2d, \dots$, where the initial term a and the common difference d are real numbers.
Examples:
1. Let $a = 1$ and $d = 4$.
 $\{a_n\} = \{a_1, a_2, a_3, a_4, \dots\} = \{1, 5, 9, 13, \dots\}$
2. Let $a = 7$ and $d = -6$.
 $\{a_n\} = \{a_1, a_2, a_3, a_4, \dots\} = \{7, 1, -5, -11, \dots\}$
3. Let $a = 1$ and $d = 2$.
 $\{a_n\} = \{a_1, a_2, a_3, a_4, \dots\} = \{1, 3, 5, 7, \dots\}$

Arithmetic Sequence Recursive Formula



The n^{th} term of an arithmetic sequence

$a_1, a_2, \dots, a_n, \dots$ is,

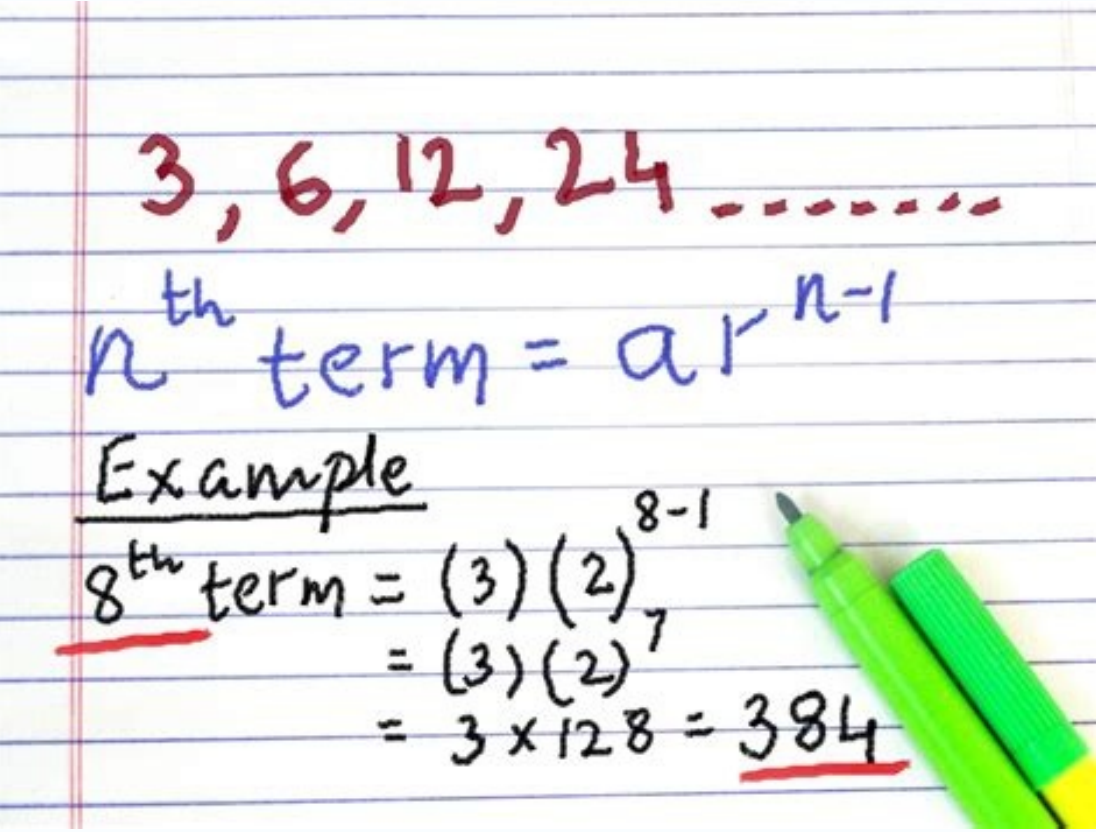
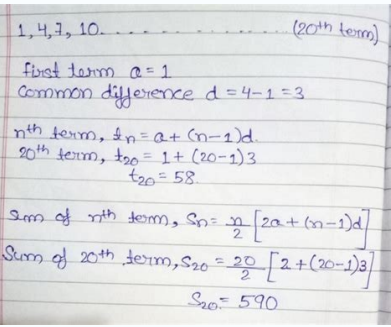
$a_n = a_{n-1} + d$, where

→ a_n = the n^{th} term

→ a_{n-1} = the $(n-1)^{\text{th}}$ term

→ d = common difference

= $a_2 - a_1$ (or) $a_3 - a_2 = \dots = a_n - a_{n-1}$



First 5 terms of an arithmetic sequence. How to find the first three terms of an arithmetic sequence. First three terms of arithmetic sequence.

This online calculator can solve arithmetic progression problems. Currently, it can help solve two types of problems: find the n th term of an arithmetic progression given the m th term and the common difference. Example problem: An arithmetic progression has a common difference of 10 and its 5th term is 52. Find its 15th term. Find the n th term of the progression given the i th and j th terms. Example problem: The 5th term of an arithmetic progression is 12 and the 15th term is 52. Find the 20th term. Some formulas and solution descriptions can be found below the calculator. The first term of the arithmetic progression The tenth term of the sequence Formula Arithmetic progression Recall that the arithmetic progression or arithmetic progression (AP) is a series of numbers, the difference of two consecutive consecutive terms, called the common difference, is one constant. Thus the formula for the n th term is of the form and in the general case where d is the common difference. You can solve the first type of problems listed above directly with the general formula or by evaluating the first term a_1 with the formula. And then by the formula of the n th term. The second type of problem is to find the common difference using the following formula derived from the general formula. Then it becomes the first type of problem. The above calculator also calculates the first term of the arithmetic progression and the general formula for the n th term for convenience. Find indices, sums and common differences of arithmetic progressions step by step Follow arithmetic progressions Our experienced online tutors can solve this problem. Get step-by-step solutions from experienced instructors in just 15-30 minutes. Your first 5 questions will go to us! In partnership with You have been directed to Course Hero I would like to submit the same question to the Course Hero Arithmetic Progression Calculator en Feedback This Arithmetic Progression Calculator (aka ArithmeticCalculator) is a useful tool for analyzing a sequence of numbers created by adding a constant value each time. You can use it to find any property of a sequence—the first term, the common difference, the n th term, or the sum of the first n terms. You can dive right in or read on to find out how it works. In this article, we explain the definition of an arithmetic sequence, explain the sequence equation used by the calculator, and provide a formula for finding an arithmetic series (the sum of an arithmetic sequence). We also provide an overview of the differences between arithmetic and geometric sequences and an easy-to-understand example of how to use our tool. To answer this question, you must first know what the term sequence means. By definition, a sequence in mathematics is a set of objects, such as numbers or letters, that are in a particular order. These objects are called sequence elements or members. Quite often the same object appears several times in a row. An arithmetic sequence is also a set of objects - more precisely numbers. Each ordinal number is created by adding a constant number (the so-called common difference) to the previous one. Such a sequence can be finite if it has a certain number of members (eg 20), or infinite if we do not specify the number of members. Each arithmetic sequence is uniquely defined by two coefficients: the common difference and the first term. Knowing these two values, the entire sequence can be written. When you start to delve into the topic of arithmetic progression, you may encounter some confusion. This is due to the different naming conventions used. Two of the most common terms you may come across are arithmetic progression and series. The former is often also called arithmetic progression, while the latter is also called partial sum. The main difference between the sequence and by definition, an arithmetic sequence is simply a set of numbers that each time results from the sum of the common difference. Arithmetic sequences, on the other hand, are the sum of n terms of the sequence. For example, you can denote the sum of the first 12 terms as $S_{12} = a_1 + a_2 + \dots + a_{12}$. Some examples of arithmetic progression: 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, ... 6, 3, 0, -3, -6, -9, -12, -15, ... 50, 50.1, 50.2, 50.3, 50.4, 50.5, ... Can you find the common difference between each of these sequences? Hint: Try subtracting one expression from the next. You can see from these examples of arithmetic sequences that the common difference doesn't have to be a whole number—it can be a fraction. In fact, it doesn't even have to be positive! If the common difference of an arithmetic sequence is positive, we call it an increasing sequence. Of course, if the difference is negative, the sequence will be descending. What happens at zero difference? Well, you get a monotonic sequence where each term is equal to the previous one. Now let's take a closer look at this sequence: 0, 1, 1, 2, 3, 5, 8, 13, 21, 34, ... Can you figure out the total difference in this case? In fact, you shouldn't. This is not an example of an arithmetic sequence, but a special case called the Fibonacci sequence. Each expression is found by adding two expressions in front of it. A great application of the Fibonacci sequence is the construction of a spiral. If you were to draw squares whose sides are equal to successive members of this sequence, you would get a perfect spiral. A perfect spiral - like this one! (Image credit: Wikimedia.) Mathematicians have always loved the Fibonacci sequence! To discover the sequence that's been scaring you for nearly a century, check out our Collatz Estimate Calculator. Suppose you want to find the 30 th term of the above sequences (except the Fibonacci sequence, of course). WriteThe first 30 conditions would be tedious and time consuming. However, you may have noticed that you don't have to save them all! Just add 29 common differences to the first word. We generalize this statement to formulate the equation of an arithmetic progression. This is the formula for each n^{th} member of the sequence. $a = a_1 + (n-1)d$, where: a is a member of the n^{th} sequence; r - total difference; i a_1 The first member of the sequence. This arithmetic progression formula applies to all ordinary differences, whether positive, negative, or zero. Of course, if the difference is zero, all the terms are equal, making any calculations superfluous. Our arithmetic sequence calculator can also calculate the sum of a sequence (called an arithmetic series) for you. Trust me, you can do it yourself - it's not that hard! Look at the first example of an arithmetic progression: 3, 5, 7, 9, 11, 13, 15, 17, 19, 21. We can add all the terms manually, but it's not necessary. Let's try to summarize the terms in a more structured way. We add the first and the last term, then the second and the second to last, the third and the third to the last, etc. You'll quickly notice: $3 + 21 = 24$ $5 + 19 = 24$ $7 + 17 = 24$ The sum of each pair is constant and equal to 24. This means we don't have to add all the numbers. All you have to do is add the first and last terms of the sequence and multiply that sum by the number of pairs (i.e. $n/2$). Mathematically, this is written as follows: $S = n/2 \cdot (a_1 + a_n)$ Substituting the arithmetic sequence equation for the term a_n : $S = n/2 \cdot (a_1 + a_1 + (n-1)d)$ Simplified: $S = n/2 \cdot (2a_1 + (n-1)d)$ You can use this formula to find the sum of an arithmetic sequence. When looking for the sum of an arithmetic progression, you've probably noticed that to calculate a running sum, you have to select n . What if you want to sum all members of a string? Intuitive so-calledAn infinite number of terms will be infinite regardless of whether the total difference is positive, negative, or even zero. However, this does not apply to all sequence types. If you choose a different sequence, e.g. a geometric sequence, the sum can be a finite term up to infinity. Of course, our arithmetic progression calculator cannot parse other types of sequences. For example, the sequence 2, 4, 8, 16, 32, ... has no common difference. This is because it is a different type of sequence - a geometric progression. What is the main difference between arithmetic progression and geometric progression? While arithmetic uses a common difference to create each successive term, geometric sequence uses a common ratio. This means that we multiply each term by a specific number every time we want to create a new term. An interesting example of a geometric sequence is the so-called digital universe. You've probably heard that the amount of digital information doubles every two years. This means you can write numbers that represent the amount of data in a geometric progression with a common factor of two. You can also analyze a special type of sequence called an arithmetic-geometric sequence. It is formed by multiplying the terms of two progressions - arithmetic and geometric. For example, consider the following two sequences: Arithmetic Series: 1, 2, 3, 4, 5 Geometric Series: 1, 2, 4, 8, 16 To get the n th term of an arithmetic-geometric series, multiply the arithmetic sequence of the n th terms through the geometric n th part of the sequence. In this case, the result is: First term: $1 \times 1 = 1$ Second term: $2 \times 2 = 4$ Third term: $3 \times 4 = 12$ Fourth term: $4 \times 8 = 32$ Fifth term: $5 \times 16 = 80$ So a sequence defines four parameters: initial value of the arithmetic sequence a , common difference d , initial value of the geometric sequence b and the general ratio r . Let's consider a simple example that can be solved using the arithmetic progression formula. Let's take a closer look at an example of free fall. The stone freely falls into a deep shaft. In the first second it moves four meters down. For every additional second, the fall distance increases by 9.8 meters. How far does the stone travel between 5 and 9 seconds? The distance traveled corresponds to an arithmetic progression with a starting value of $a = 4$ m and a total difference of $d = 9.8$ m. First, we calculate the total distance traveled in the first nine seconds of free fall by assuming S_9 (n = 9) calculate: $S_9 = n/2 \cdot (2a + (n-1)d) = 9/2 \times (2 \times 4 + (9-1) \times 9.8) = 388.8$ m In the first nine seconds, the stone back a total of 388.8 m. However, we are only interested in the distance traveled between the fifth and the ninth second. How to calculate this value? Very simple - just subtract the distance S_4 covered in the first four seconds from the subtotal S_9 . $S_9 = n/2 \cdot (2a + (n-1)d) = 4/2 \times (2 \times 4 + (4-1) \times 9.8) = 74.8$ m S_4 equals 74.8 m. Let us find now the result is simply subtraction: Distance = $S_9 - S_4 = 388.8 - 74.8 = 314$ m. There is an alternative method to solve this example. Using the arithmetic sequence formula, you can calculate the distance traveled in the fifth, sixth, seventh, eighth, and ninth seconds and add these values. Try it yourself - you'll quickly find out that the effect is exactly the same! To find the term a_n of an arithmetic progression, a_n : Multiply the common difference d by $(n-1)$. Add this product to the first term a_1 . The result is the term a_n . Very good! You can also use the formula: $a_n = a_1 + (n-1) \cdot d$. Subtract any two adjacent terms to get the common sequence difference. You can use any of the following characters, such as B . $a_1 - a_2$, $a_2 - a_3$ or $a_4 - a_5$. UnlessSame result for all differences, their order is not arithmetic. The total difference is 11. You can estimate this by subtracting any pair of consecutive terms, for example $a_4 - a_5 = -1 - (-12) = 11$ or $a_1 - a_2 = 21 - 10 = 11$. The difference between adjacent terms is constant for any arithmetic sequence, while the ratio of each pair of consecutive terms is the same for any geometric sequence. To get the next term of an arithmetic progression, you need to add the common difference from the previous one. To obtain the next term of a geometric sequence, the previous term must be multiplied by a common factor. The difference between two consecutive numbers must be the same. To check that a sequence is arithmetic, find the differences between each pair of adjacent terms. If any of the values are different, your sequence is not arithmetic. Arithmetic.

